

(14) Today

4.1 Symmetry elements and Operations

4.2 Point Groups

4.3 Properties and Representations of Groups

(16) Second Class from Today

4.3 Properties and Representations of Groups

4.4 Uses of Character Tables

Next Class (15)

4.3 Properties and Representations of Groups

Third Class from Today (17)

4.4 Uses of Character Tables

1

Chap 5

Character Tables
Irreducible representation

Summary of all the symmetry
symmetry operations

Section 4.3

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	Z axis	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z same	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz

matching functions
Same symmetry
as moving
something
along the z axis

characters
Multiplets - symmetry labels

σ bond
 π bond
label that describes
the symmetry of the
bond

same symmetry as rotating something
or the z axis

What can we use character tables for?

Section 4.4

anything that relates to symmetry

How do we use Character Tables.

To examine the symmetry of the thing we are interested in (molecular motions, orbitals, symmetry adapted linear combinations of atomic orbitals...) we create a reducible representation of the symmetry elements of the thing we are interested in.

We use linear algebra to determine the irreducible representations that must be combined to form the reducible one that we just found.

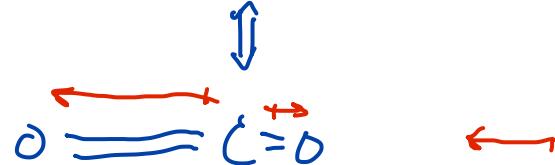
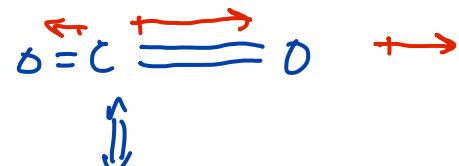
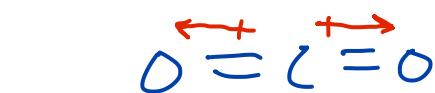
We use the functions in the character tables to interpret our results.

For each operation add 1, 0 or -1 to the value for χ based on whether there is no change (1), the item changes position (0), or doesn't change position but changes sign (-1).

Infrared Spectroscopy vibrational spectroscopy

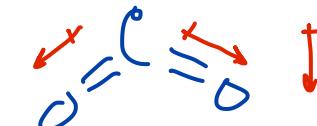
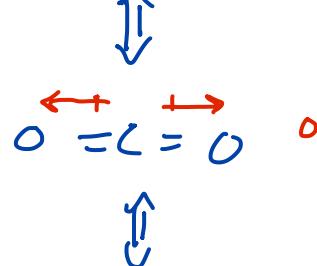
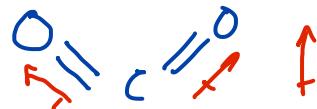
Review

a vibration that changes the dipole of the molecule can interact with and absorb IR light



IR active

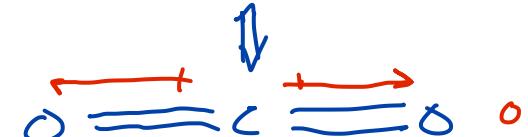
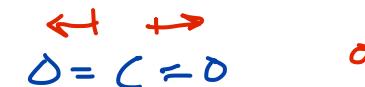
stretching mode



IR active

this one but
out of the
plane

bending mode



not IR active

stretching mode

Things we are interested in: ... atomic motions of the atoms in a molecule

Number of IR Active Vibrational Modes for Water

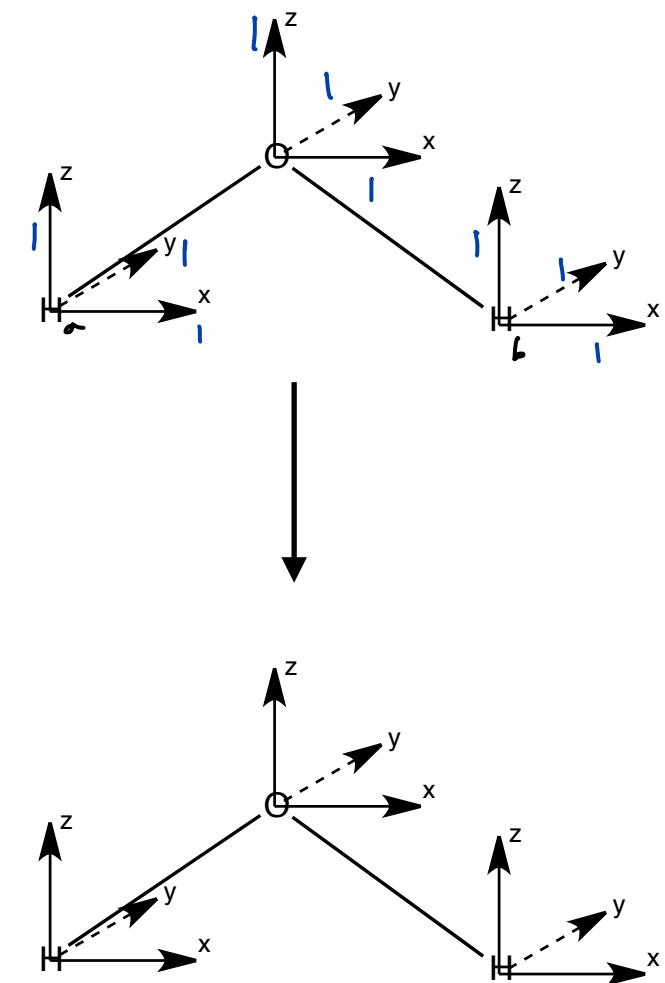
Section 4.4

C_{2v}	E	C_2	$\sigma_{(xz)}$	$\sigma_{(yz)}$
Γ	9			

$$H_a = \begin{matrix} O & x'_o & y'_o & z'_o & x'_{Ha} & y'_{Ha} & z'_{Ha} & x'_{Hb} & y'_{Hb} & z'_{Hb} \\ & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ & y'_o & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ & z'_o & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ H_a & x'_{Ha} & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ & y'_{Ha} & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ & z'_{Ha} & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ & x'_{Hb} & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ & y'_{Hb} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ & z'_{Hb} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{matrix} \quad \begin{matrix} x_o & y_o & z_o & x_{Ha} & y_{Ha} & z_{Ha} & x_{Hb} & y_{Hb} & z_{Hb} \end{matrix}$$

trace of this matrix is 9

the sum of the diagonal elements



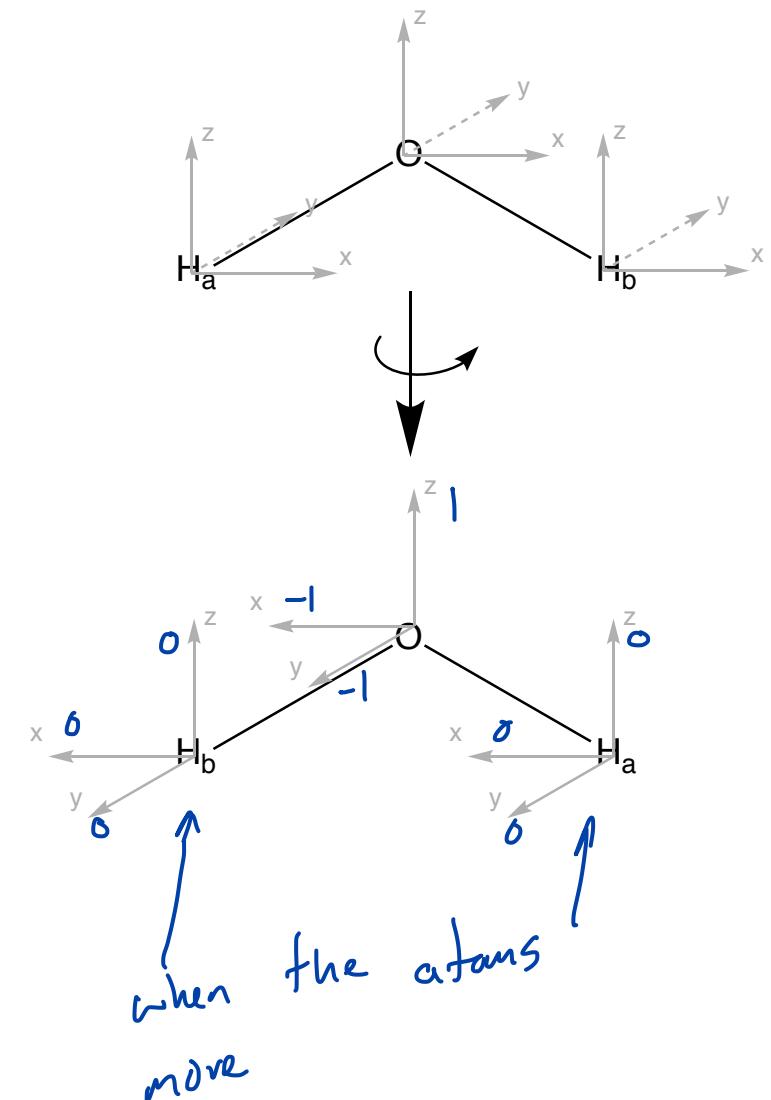
Number of IR Active Vibrational Modes for Water

Section 4.4

C_{2v}	E	C_2	$\sigma_{(xz)}$	$\sigma_{(yz)}$
	9	-1		

$$\begin{array}{l}
 \text{O} \quad x'_o \quad -1 \\
 \text{y}'_o \quad -1 \\
 \text{z}'_o \quad 1 \\
 \\
 \text{H}_a \quad x'_{\text{Ha}} \quad 0 \\
 \text{y}'_{\text{Ha}} \quad 0 \\
 \text{z}'_{\text{Ha}} \quad -1 \\
 \\
 \text{H}_b \quad x'_{\text{Hb}} \quad 0 \\
 \text{y}'_{\text{Hb}} \quad -1 \\
 \text{z}'_{\text{Hb}} \quad 1
 \end{array} = \begin{array}{cccccc}
 & x_o & y_o & z_o & x_{\text{Ha}} & y_{\text{Ha}} & z_{\text{Ha}} \\
 x'_o & -1 & & & 0 & & 0 \\
 y'_o & & -1 & & & & \\
 z'_o & & & 1 & & & \\
 \\
 x'_{\text{Ha}} & 0 & & & -1 & & \\
 y'_{\text{Ha}} & & 0 & & & -1 & \\
 z'_{\text{Ha}} & & & 0 & & & 1 \\
 \\
 x'_{\text{Hb}} & 0 & & & 0 & & \\
 y'_{\text{Hb}} & -1 & & & & 0 & \\
 z'_{\text{Hb}} & 1 & & & & & 0
 \end{array}$$

trace $-1 + -1 + 1$

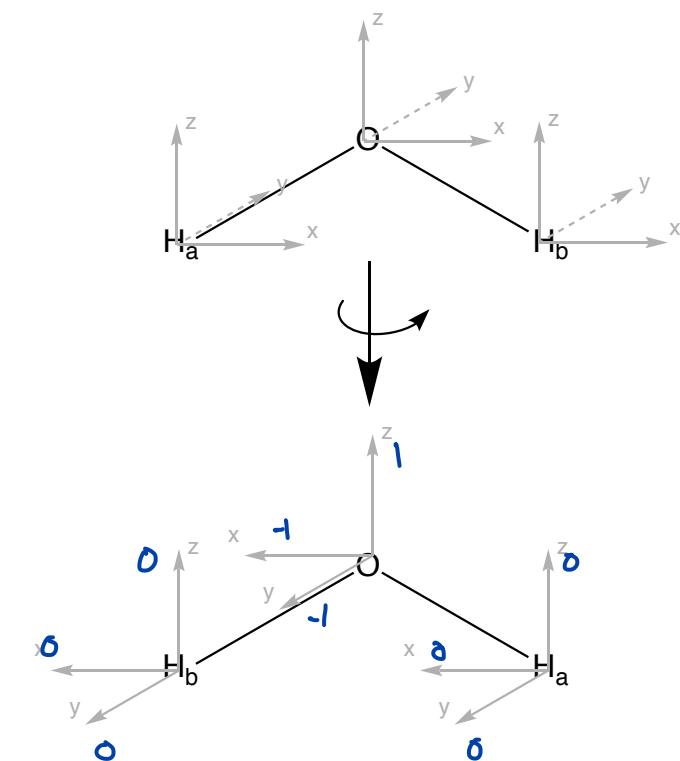


Easier way to determine the trace?

Section 4.4

C_{2v}	E	C_2	σ_{xz}	σ_{yz}
	9	-1		

O	x'_o	-1			x_o
	y'_o		-1		y_o
	z'_o			1	z_o
H _a	x'_{Ha}		0	-1	x_{Ha}
	y'_{Ha}		0	-1	y_{Ha}
	z'_{Ha}		0	1	z_{Ha}
H _b	x'_{Hb}	-1	0	0	x_{Hb}
	y'_{Hb}		-1	0	y_{Hb}
	z'_{Hb}		1	0	z_{Hb}

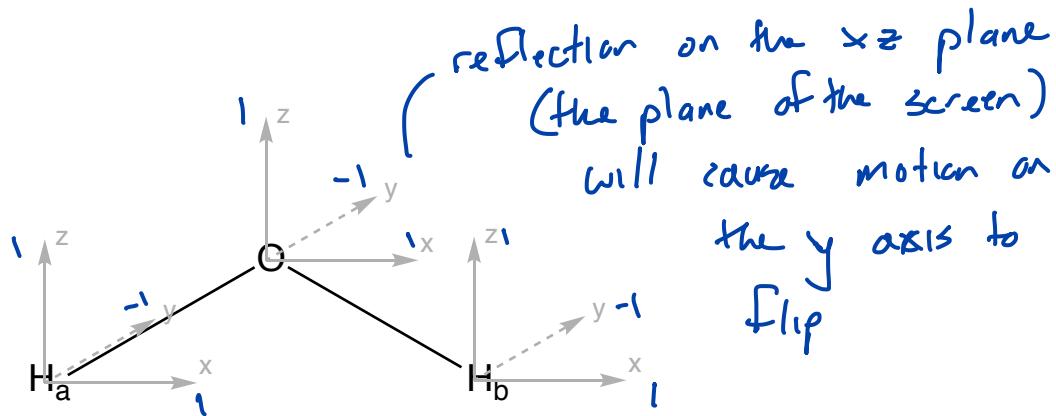


For each operation add 1, 0 or -1 to the value for χ based on whether there is no change (1), the items changes position (0), or doesn't change position but changes sign (-1).

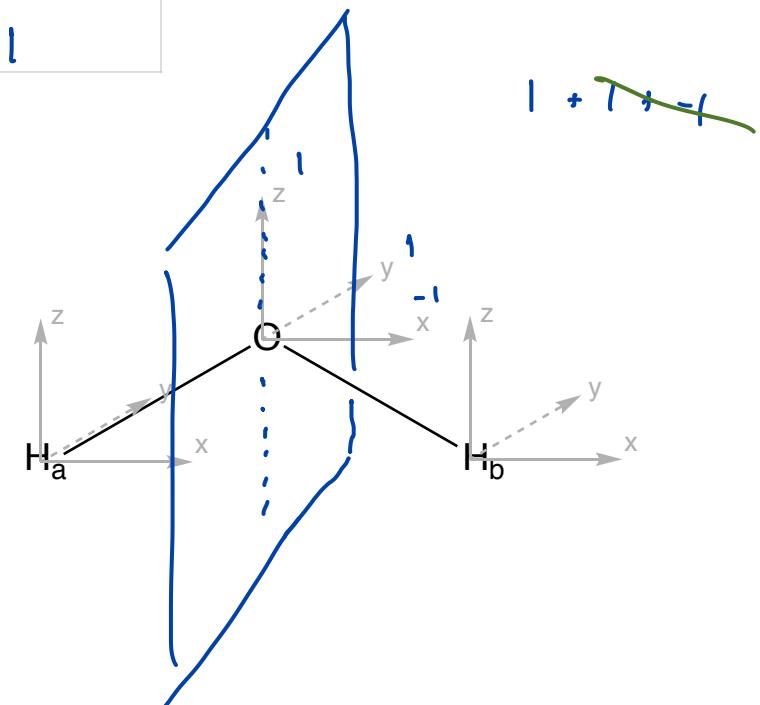
Number of IR Active Vibrational Modes for Water

Section 4.4

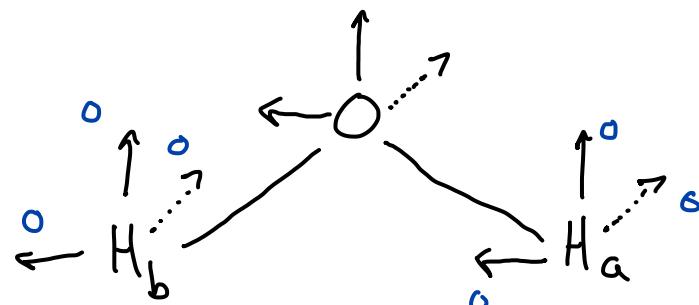
C_{2v}	E	C_2	$\sigma(xz)$	$\sigma(yz)$
Γ	9	-1	3	1



$| + -1 + | + | + -1 + | + | + -1 + |$



For each operation add 1, 0 or -1 to the value for χ based on whether there is no change (1), the items changes position (0), or doesn't change position but changes sign (-1).



C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	9	-1	3	1		

now that we have the reducible representation we need to find which irreducible representations are used to make it

Extracting the Symmetry in formation by reducing the reducible representation

Section 4.4

number of irreducible representations of a given type needed

$$= \frac{1}{\text{order}} \sum_{\text{classes}} \left[\begin{pmatrix} \# \\ \text{operations} \\ \text{in class} \end{pmatrix} \begin{pmatrix} \chi \text{ of the} \\ \text{irreducible} \\ \text{representation} \end{pmatrix} \begin{pmatrix} \chi \text{ of the} \\ \text{reducible} \\ \text{representation} \end{pmatrix} \right]$$

sum of the squares of the characters under E

or sum across all classes

class



$$n(A_1) = \frac{1}{4} \cdot [(1)(1)(9) + (1)(1)(-1) + (1)(1)(3) + (1)(1)(1)]$$

$n = 3$

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	9	-1	3	1		

number of
irreducible
representations = $\frac{1}{\text{order}} \sum_{\text{classes}} \left[\begin{pmatrix} \# \\ \text{operations} \\ \text{in class} \end{pmatrix} \begin{pmatrix} \chi \text{ of the} \\ \text{irreducible} \\ \text{representation} \end{pmatrix} \begin{pmatrix} \chi \text{ of the} \\ \text{reducible} \\ \text{representation} \end{pmatrix} \right]$

$$n(A_2) = \frac{1}{4} \cdot [(1)(1)(1) + (1)(-1)(-1) + (-1)(-1)(1) + (-1)(1)(-1)]$$

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	9	-1	3	1		

number of
irreducible
representations = $\frac{1}{\text{order}} \sum_{\text{classes}} \left[\begin{pmatrix} \# \\ \text{operations} \\ \text{in class} \end{pmatrix} \begin{pmatrix} \chi \text{ of the} \\ \text{irreducible} \\ \text{representation} \end{pmatrix} \begin{pmatrix} \chi \text{ of the} \\ \text{reducible} \\ \text{representation} \end{pmatrix} \right]$

$$n(B_1) = \frac{1}{6} \cdot [(1)(1)(1) + (1)(-1)(1) + (-1)(1)(1) + (1)(-1)(-1)]$$

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	9	-1	3	1		

number of
irreducible
representations = $\frac{1}{\text{order}} \sum_{\text{classes}} \left[\begin{pmatrix} \# \\ \text{operations} \\ \text{in class} \end{pmatrix} \begin{pmatrix} \chi \text{ of the} \\ \text{irreducible} \\ \text{representation} \end{pmatrix} \begin{pmatrix} \chi \text{ of the} \\ \text{reducible} \\ \text{representation} \end{pmatrix} \right]$

$$n(B_2) = \frac{1}{6} \cdot [(1)(1)(1) + (1)(-1)(-1) + (-1)(-1)(1) + (-1)(1)(-1)]$$

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz
Γ	9	-1	3	1		

C _{2v}	E	C ₂	σ _v (xz)	σ _v (yz)		
A ₁	1	1	1	1	z	x ² , y ² , z ²
A ₂	1	1	-1	-1	R _z	xy
B ₁	1	-1	1	-1	x, R _y	xz
B ₂	1	-1	-1	1	y, R _x	yz
Γ	9	-1	3	1		

$$\Gamma = 3A_1 + A_2 + 3B_1 + 2B_2$$

all possible motions = vibration + translation + rotation

$$\text{number of vibrational modes} = \left(\begin{array}{l} \# \text{ of ways} \\ \text{of moving} \end{array} \right) - \left(\begin{array}{l} \text{translational} \\ \text{movement} \end{array} \right) - \left(\begin{array}{l} \text{rotational} \\ \text{movement} \end{array} \right)$$

